## Geometry R WS 4.7 Isosceles and Equilateral Triangles

Name	
Date	Period

Ex. 8

- 1. In  $\triangle ABC$ , if  $\overline{CA} \cong \overline{CB}$  and  $m \angle A = 50$ , find  $m \angle B$ .
- **2.** In  $\triangle ABC$ ,  $\overline{AB} \cong \overline{BC}$ . If AB = 5x and BC = 2x + 18, find AB and BC.
- 3. In isosceles triangle ABC,  $\overline{AB} \cong \overline{BC}$ . If AB = 5x + 10, BC = 3x + 40, and AC = 2x + 30, find the length of each side of the triangle.
- **4.** In  $\triangle ABC$ ,  $\overline{AB} \cong \overline{BC}$ . If  $m \angle A = 7x$  and  $m \angle C = 2x + 50$ , find  $m \angle A$  and  $m \angle C$ .
- 5. In  $\triangle EFG$ ,  $\overline{EF} \cong \overline{FG}$ . If  $m \angle E = 4x + 50$ ,  $m \angle F = 2x + 60$ , and  $m \angle G = 14x + 30$ , find  $m \angle E$ ,  $m \angle F$ , and  $m \angle G$ .





- 7. Given: Isosceles triangles ABC and ADC have common base  $\overline{AC}$ . Prove:  $\angle BAD = \angle BCD$ .
- 8. If  $\overline{CA} \cong \overline{CB}$ , and  $\overline{DA} \cong \overline{EB}$ , prove that  $\angle 1 \cong \angle 2$ .



- **9.** Given: In  $\triangle ABC$ ,  $\overline{CA} \cong \overline{CB}$ ,  $\overline{AR} \cong \overline{BS}$ ,  $\overline{DR} \perp \overline{AC}$ , and  $\overline{DS} \perp \overline{BC}$ . *Prove:*  $\overline{DR} \cong \overline{DS}$ .
- 10. In isosceles triangle ABC, D and F are midpoints of the congruent legs, and E and G are the trisection points of the base ( $\overline{AE} \cong \overline{EG} \cong \overline{GB}$ ). Prove that  $\overline{DE} \cong \overline{FG}$ .
- 11. Given RPQT,  $SR \cong ST$ , and  $\angle 1 \cong \angle 2$ , prove that  $\triangle PSQ$  is an isosceles triangle.



- **12.** In  $\triangle ABC$ ,  $\overline{AB} \cong \overline{AC}$ ,  $\overline{DE} \perp \overline{BC}$ ,  $\overline{FG} \perp \overline{BC}$ , and  $\overline{BG} \cong \overline{CE}$ . Prove that  $\overline{BD} \cong \overline{CF}$ .
- **13.** Given  $\overline{AD} \cong \overline{BE}$ ,  $\overline{CD} \cong \overline{CE}$ , and  $\overline{ADEB}$ , prove that  $\overline{AC} \cong \overline{BC}$ .
- 14. If  $\triangle ABC$  is an equilateral triangle and  $\overline{CT} \cong \overline{AR} \cong \overline{BS}$ , prove:

**a.**  $\overline{TA} \cong \overline{RB} \cong \overline{SC}$ **b.**  $\triangle TAR \cong \triangle RBS \cong \triangle SCT$ **c.**  $\overline{TR} \cong \overline{RS} \cong \overline{ST}$ **d.**  $\triangle TRS$  is an equilateral triangle.